General Method to Predict Voltage-Dependent Ionic Conduction in a Solid Electrolyte Coating on Electrodes

Jie Pan  
*University of Kentucky, jie.pan@uky.edu*

Yang-Tse Cheng  
*University of Kentucky, yang.t.cheng@uky.edu*

Yue Qi  
*Michigan State University*

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General method to predict voltage-dependent ionic conduction in a solid electrolyte coating on electrodes

Jie Pan* and Yang-Tse Cheng†
Department of Chemical and Materials Engineering, University of Kentucky, Lexington, Kentucky 40506-0046, USA

Yue Qi‡
Department of Chemical Engineering and Materials Science, Michigan State University, East Lansing, Michigan 48824-1226, USA

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Understanding the ionic conduction in solid electrolytes in contact with electrodes is vitally important to many applications, such as lithium ion batteries. The problem is complex because both the internal properties of the materials (e.g., electronic structure) and the characteristics of the externally contacting phases (e.g., voltage of the electrode) affect defect formation and transport. In this paper, we developed a method based on density functional theory to study the physics of defects in a solid electrolyte in equilibrium with an external environment. This method was then applied to predict the ionic conduction in lithium fluoride (LiF), in contact with different electrodes which serve as reservoirs with adjustable Li chemical potential (μLi) for defect formation. LiF was chosen because it is a major component in the solid electrolyte interphase (SEI) formed on lithium ion battery electrodes. Seventeen possible native defects with their relevant charge states in LiF were investigated to determine the dominant defect types on various electrodes. The diffusion barrier of dominant defects was calculated by the climbed nudged elastic band method. The ionic conductivity was then obtained from the concentration and mobility of defects using the Nernst-Einstein relationship. Three regions for defect formation were identified as a function of μLi: (1) intrinsic, (2) transitional, and (3) p-type region. In the intrinsic region (high μLi, typical for LiF on the negative electrode), the main defects are Schottky pairs and in the p-type region (low μLi, typical for LiF on the positive electrode) are Li ion vacancies. The ionic conductivity is calculated to be approximately 10⁻³¹ S cm⁻¹ when LiF is in contact with a negative electrode but it can increase to 10⁻¹² S cm⁻¹ on a positive electrode. This insight suggests that divalent cation (e.g., Mg²⁺) doping is necessary to improve Li ion transport through the engineered LiF coating, especially for LiF on negative electrodes. Our results provide an understanding of the influence of the environment on defect formation and demonstrate a linkage between defect concentration in a solid electrolyte and the voltage of the electrode.

I. INTRODUCTION

The origin of ionic conduction in solid electrolytes is defect formation and transport in ionic materials [1–4]. At a defined temperature, the internal equilibria of defects depend on two aspects: (1) the atomic structure of the defects and (2) the electronic band structure of the material [3,5,6]. However, in reality, an ionic material of interest always operates in an environment (e.g., PbO in oxygen gas [3]; Li ionic conductors coated on electrodes). In this situation, due to the formation of defects, the compound can deviate from the exact stoichiometric composition. As a result, the concentration of defects varies with the environment in which the ionic material is in a thermodynamic equilibrium [3]. For example, by increasing the partial oxygen pressure \( P_O^2 \) (equivalently chemical potential of oxygen \( \mu_{O^2} = \mu_{O^2} + RT \ln \frac{P_{O^2}}{P_{O^2_0}} \) [3]) passing over PbO, the concentration of oxygen vacancies decreases while that of the oxygen interstitials increases as depicted in the Kröger-Vink or Brouwer diagram [3,5]. Therefore, the environment can be treated as a “tuner” that can change the concentrations of defects in a material. In general, the environment is not only limited to the gas phase, but can be liquid or solid phase, such as electrodes on which the solid electrolyte is coated. Similarly, the concentrations of defects in the solid electrolyte would be electrode voltage dependent according to the Nernst equation \( [V = -\frac{1}{F} (\mu_{Li}^{\text{cathode}} - \mu_{Li}^{\text{anode}})] \) [7]. The goal of this work is to develop a method to study defect physics and, thus, ionic conduction in a material in contact with an external environment, e.g., a solid electrolyte on various electrodes for lithium ion batteries (LIBs).

Recently, solid electrolytes attracted a lot of research emphasizes not only because the promising future of all-solid batteries [4,8–16], but also due to their importance as an interfacial layer between electrodes and liquid electrolytes, known as a solid electrolyte interphase (SEI) [17,18]. The performance of liquid electrolyte based LIBs relies on forming a stable SEI on the electrode surface [17,18]. In theory, an ideal SEI is expected to be ionic conducting [19–21], electrical insulating [22–24], and mechanically stable [25,26]. However, the characters of a natural SEI depend on many factors (e.g., property of electrode and electrolyte molecules) and a stable passivating layer is not always formed. For example, silicon (Si) electrode, one of the most promising negative electrodes with the highest theoretical capacity [27], cannot maintain a stable interphase [26] due to its large volume expansion [28–31]. This leads to a continuous capacity loss and degradation of the battery. Recently, surface coatings [32–35] and electrolyte additives [36] have been proposed as two promising ways to modify SEIs. In the first approach, surface
coatings, such as Al2O3, TiO2, and AlF3, have been designed to serve as an artificial SEI to mitigate electrochemical and mechanical degradation of the electrodes [32–35,37,38]. It was believed that solid electrolyte thin film coatings, also known as engineered artificial SEIs, were more stable than naturally formed SEIs in maintaining passivation, preventing continuous liquid electrolyte molecule decomposition, and protecting the electrodes from further degradation [32–35].

The second approach, by adding small amounts of electrolyte additives (e.g., vinylene carbonate [39,40], fluoroethylene carbonate [41–47]), the performance of the electrodes was improved with a longer cycling life. The additives have been shown to change the inorganic components in the SEI (e.g., increased formation of lithium fluoride) [41–47]. The mechanisms responsible for the two promising approaches are not well understood. A theoretical approach is therefore needed to understand the mechanism of ionic and electronic conduction in SEI components.

A theoretical method to understand ionic conduction in a solid electrolyte should include two parts: (1) the concentration of defects in the solid electrolyte in contact with electrodes and (2) the transport of the dominant defects (e.g., Li vacancy).

The dependence of charged defect reactions on the chemical potential of electrons (i.e., Fermi energy) has been observed in various material systems [48–51]. More generally, Zhang and Northrup [52] developed a first principles based method and demonstrated that defect concentration is a function of the chemical potential of atomic constituents. This formalism has been successfully applied to study multiple defect physics, e.g., defect compensation in ZnSe [53], zinc vacancies as the dominant intrinsic acceptor defects in ZnO [54], and nitrogen vacancies as the dominant intrinsic donor defects in p-type GaN [55]. In 2004, Van de Walle and Neugebauer [56] published a comprehensive review article on this method and its applications to study defect physics in III-nitrides.

However, to benefit battery design, it is necessary to link defect reactions to an electrochemically measurable parameter, such as the open circuit voltage of the electrode. In this work, we extended this method [52–56] based on density functional theory to calculate the ionic conductivity in a solid electrolyte on electrodes. In our approach, electrodes are modeled as lithium (Li) reservoirs with a range of Li chemical potential on electrodes. In our approach, electrodes are modeled as lithium (Li) reservoirs with a range of Li chemical potential on electrodes.

In this study, our interest focuses on ionic conduction in LiF coated on various electrodes with rigorous considerations of the remaining technical challenges. LiF is one of the promising engineered SEI coating materials on the electrodes (e.g., Si) of LIBs, since the improved performance of electrodes has been linked to the increased concentration of LiF in the natural SEI [41–47,57]. In addition, perfect LiF crystals have a wide band gap [58–60], and can thus block the electron leakage to the electrolyte from the electrodes.

II. METHODOLOGY

A. Thermodynamics of defects

In ionic crystals, typical types of defects include interstitials, vacancies, Frenkel pairs, and Schottky pairs [1–3]. Table I summarizes possible defects with various charge states in LiF and their notations used in this paper. In our model, defects are equilibrated with external Li reservoirs (known as external defect equilibria [3], in which deviation from the exact stoichiometric composition is allowed). As a result, the formation energy of a defect i with charge q is defined

TABLE I. Summary of defect types in LiF.

<table>
<thead>
<tr>
<th>Notation (i)</th>
<th>Kröger-Vink notation [3,5,6]</th>
<th>Defect types</th>
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<td>Li+</td>
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<td>Li2+</td>
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The formation energies of paired defects (Frenkel pair and Schottky pair) are dependent on their distances of separation. For each type of pair, the formation energies of the nearest-, second nearest-, and third nearest-neighbor pairs were calculated and the one with the lowest formation energy was included in Eq. (3). In addition, another scenario is the dilute pair (noninteracting) when two dilute point defects (e.g., V Li, F Li) have the same formation energy.
where \( E_{\text{tot}}(i,q) \) and \( E_{\text{tot}}^{\text{bulk}} \) are the calculated energies for the LiF supercell with and without one defect \( i \). \( E_V \) (\( E_V = 0 \)) is the valence band top of the bulk LiF. \( \Delta V \) is the electrostatic energy correction term to align the valence band maximum of the defected cells with that in the bulk LiF [53,56]. \( n_{Li} \) (\( n_{F} \)) is defined as the number of different Li (F) atoms compared with imperfect and perfect LiF supercells (e.g., for Li\(_i\), \( n_{Li} = 1 \) and \( n_{F} = 0 \)). \( \mu_{Li} \) and \( \mu_{F} \) are the chemical potential of Li and F in their reservoirs. In our calculation, \( \mu_{Li} \) is a free parameter depending on the properties of coated electrodes; \( \mu_{F} \) is approximated by assuming that LiF is the most stable compound for F to form

\[
\mu_{F} = \mu_{LiF} - \mu_{Li},
\]

where \( \mu_{LiF} \) is the chemical potential of LiF in our study. In Eq. (1) [56], \( \mu_{Li} \) depends on the electrode on which LiF is coated, i.e., LiF coated on the anode or cathode. On the one hand, we consider that LiF is subjected to an upper bound when LiF is coated on Li metal: \( \mu_{Li}^{\text{max}} = \mu_{Li}^{\text{metal}} = -2.02 \text{ eV} \). If we push \( \mu_{Li} \) higher, Li metal would be deposited with \( F^- \) ion dissolved in electrolyte. On the other hand, the lower bound is considered when LiF is coated on the cathode: \( \mu_{Li}^{\text{min}} = \mu_{LiF} - \mu_{F}^{\text{gas}} = -9.71 \text{ eV} \). Under this extreme condition, \( F_2 \) gas would be generated with \( Li^+ \) dissolved in the electrolyte. However, for battery applications, the typical \( \mu_{Li} \) is higher than this limit (i.e., \( \mu_{Li} \approx -6.6 \text{ eV} \) corresponding to about 4.6 volts against Li metal) [61]. As a result, we use \( \mu_{Li} \approx -6.6 \text{ eV} \) as \( \mu_{Li}^{\text{min}} \) in our study.

The Fermi energy \( \epsilon_F \), which is an unknown parameter, is referenced to the valence band top in Eq. (1). In perfect LiF, the Fermi level lies in the middle of the band gap; however, defects can create additional states in the band gap and vary the Fermi level. In our calculation, \( \epsilon_F \) is determined by imposing the charge neutrality [20,21,52] by balancing free electrons \( (n_\oplus) \), free holes \( (n_\ominus) \), and charged defects

\[
\sum_i q_i S(i,q) = n_\oplus - n_\ominus,
\]

where \( S(i,q) \) and \( q_i \) are the concentration and the associated charge of defect species, \( i \), respectively. For pairs (e.g., Frenkel and Schottky pairs), there are energy penalties to separate the nearest-neighbor pairs (e.g., for SP, the pair with 2.52 Å farther away in distance has ~0.3 eV higher in formation energy). Therefore, only the nearest-neighbor Frenkel (Schottky) pairs were included in charge balancing. At thermodynamic equilibrium, the concentration of defect \( i \) with formation energy \( E_f(i,q) \) at a finite temperature \( T \) is

\[
S(i,q) = N_s(i)e^{-E_f(i,q)/k_BT},
\]

where \( N_s(i) \) is the number of sites where defect \( i \) can be generated per unit volume. \( n_\oplus \) (\( n_\ominus \)) are the concentration of electrons (holes) in the conduction (valence) band. At a given temperature, they are defined as

\[
n_\oplus = \int_{E_C}^{E_V} \text{d}\varepsilon f(\varepsilon)D(\varepsilon),
\]

\[
n_\ominus = \int_{-\infty}^{E_C} \text{d}\varepsilon (1 - f(\varepsilon))D(\varepsilon),
\]

where \( E_C \) (\( E_V \)) is the bottom (top) of the conduction (valence) band, \( f(\varepsilon) = 1/(1 + \exp(-\varepsilon/k_BT)) \) is the Fermi-Dirac distribution, and \( D(\varepsilon) \) is the calculated electronic density of states. Since, for LiF, \( \varepsilon - \epsilon_F \gg k_BT \) \((T = 300 \text{ K} \text{ in our calculation})\), Eq. (5) can be approximated by

\[
n_\oplus = N_C e^{-(\epsilon_F - \epsilon_F)/k_BT},
\]

\[
n_\ominus = N_V e^{-(\epsilon_F - \epsilon_V)/k_BT},
\]

where \( N_C(N_V) \) is the effective density of states in the conduction (valence) band

\[
N_C = \int_{E_C}^{E_V} \text{d}\varepsilon e^{-(\epsilon_F - \epsilon_C)/k_BT} D(\varepsilon),
\]

\[
N_V = \int_{E_C}^{E_V} \text{d}\varepsilon e^{-(\epsilon_F - \epsilon_V)/k_BT} D(\varepsilon).
\]

For materials with wide band gaps (e.g., alkali halides), only the energy levels near the bottom (top) of the conduction (valence) band can be occupied (unoccupied). Therefore, we approximate \( N_C(N_V) \) as

\[
N_C \approx \int_{E_C}^{E_C + \Delta} \text{d}\varepsilon D(\varepsilon),
\]

\[
N_V \approx \int_{E_V - \Delta}^{E_V} \text{d}\varepsilon D(\varepsilon),
\]

where \( \Delta \) is a small energy interval above the conduction band (below the valence band for \( N_V \)).

### B. Defect diffusion and ionic conduction

The ionic conductivity in ionic materials depends on both the formation and the diffusion of defects [3]. The flux density of a defect \( (i,q) \) under a concentration gradient and a potential gradient can be described as the sum of Fick’s and Ohm’s law [3]

\[
\textbf{j}(i,q) = -\frac{S(i,q)D(i,q)}{RT} (\nabla \ln S(i,q) + q F \nabla \phi),
\]

where \( D(i,q) \) is the diffusion coefficient of the defect \( (i,q) \), \( F \) is the Faraday constant, and \( \phi \) is the electric potential. \( D(i,q) \) can be calculated by Arrhenius equation at a finite temperature \( T \) [62]

\[
D(i,q) = g f \nu^* (\Delta x)^2 \exp(-E_m(i,q)/k_BT) \approx \frac{1}{2} \nu^* (\Delta x)^2 \exp(-E_m(i,q)/k_BT),
\]

where \( \nu^* \) is the typical phonon frequency (e.g., \( \nu^* \approx 10^{13} \text{ Hz} \text{ along [110] direction [63]} \)), \( \Delta x \) is the net travel distance in each hop, \( g \) is the geometric factor, \( f (f = \frac{1 + \sum_j Q_j \cos \theta_j}{1 - \sum_j Q_j \cos \theta_j}) \) [64], where \( Q_j \) is the jumping possibility along angle \( \theta_j \), is the correlation factor, and \( E_m(i,q) \) is the diffusion barrier of the defect \( (i,q) \). For 1D diffusion approximation (i.e., \( V_{Li}^- \)
diffuses along [110] direction), \( \sum_{j=1}^{3} Q_j \cos \theta_j = \frac{1}{2} \cos(0) + \cos(\pi) = 0 \) and \( g = \frac{1}{2} \).

By assuming that the concentration of defects is spatially uniform, the flux density depends only on the applied potential gradient

\[
j(i,q) = -q F \frac{S(i,q)D(i,q)}{RT} \nabla \phi. \tag{11}
\]

Multiplying \( q F \) to both sides of Eq. (11), the flux density \( j(i,q) \) is converted to the current density

\[
I(i,q) = -q^2 F^2 \frac{S(i,q)D(i,q)}{RT} \nabla \phi. \tag{12}
\]

From Eq. (12), we can calculate the contribution of defect \( (i,q) \) to ionic conduction by

\[
\sigma(i,q) = -\frac{I(i,q)}{\nabla \phi} = \frac{q^2 F^2 S(i,q)D(i,q)}{RT}, \tag{13}
\]

and the total ionic conduction is the sum of the contributions from main defects in the system

\[
\sigma = \sum_i \sigma(i,q). \tag{14}
\]

C. Computational details

In this study, the energies and electronic density of states were calculated by density functional theory (DFT) with plane wave basis sets in the Vienna ab initio simulation package (VASP) [65,66]. The exchange-correlation functional was approximated by the generalized gradient approximation (GGA) in the Perdew-Burke-Ernzerhof (PBE) flavor [67]. Projector-augmented-wave (PAW) potentials were used to mimic the ionic potentials [68]. The crystal LiF has the sodium chloride face-centered cubic structure (space group: \( Fm\bar{3}m \), No. 225 [2,69]) and the structure was optimized with the total energy converged to \( 10^{-5} \) eV/supercell. A \( 3 \times 3 \times 3 \) supercell was used in the optimization with a cutoff energy of 480 eV for the plane wave basis sets, a \( 3 \times 3 \times 3 \) Monkhorst-Pack \( k \)-point mesh, and Fermi smearing with 0.05 eV width. The lattice constant of LiF after the optimization is 4.07 Å and the error is within 1.3% compared with experimental results [70].

The ground state energy \( E_{\text{tot}}(i,q) \) of defect \( i \) with charge \( q \) and \( E_{\text{bulk}}^{\text{LiF}} \) of the perfect LiF cell were calculated in the VASP-optimized \( 3 \times 3 \times 3 \) LiF supercell which is large enough to satisfy the dilute defect condition. To account for interactions from image defects or charges, we studied the scaling behavior of \( \Delta E = E_{\text{tot}}(i,q) - E_{\text{bulk}}^{\text{LiF}} \) of three representative cases: Li\(_i\) (zero charge), \( V_{\text{Li}}^- \) (one negative charge), and \( V_{\text{F}}^+ \) (one positive charge). The local structure of the same point defect of \( 3 \times 3 \times 3 \) LiF supercell was identical to that in \( 4 \times 4 \times 4 \) supercell calculation and the difference in \( \Delta E \) was less than 2%. The charged defects were modeled by adding (for negatively charged defects) or subtracting (for positively charged defects) one hydrogen atom to/from the total valence electrons in the supercell. In this study, the electrostatic energy correction \( (\Delta V \approx 0.03 \text{ eV}) \) was obtained from the average electrostatic energy difference between the defected cell (e.g., \( V_{\text{Li}}^- \)) and the perfect cell [53,71,72]. We noted that there are other methods to estimate \( \Delta V \), e.g., by inspecting the electrostatic potential far away from the charged defect [56]. The values of \( \Delta V \) obtained from different methods are within the same orders of magnitude (\( 10^{-2} \) eV) and the choice of \( \Delta V \) does not change the magnitude of defect concentrations. In addition, a similar magnitude of \( \Delta V \) has been observed in the literature [71] for other ionic materials. A neutralization jellium background charge was assumed by VASP to improve the energy convergence with respect to the supercell size [73–75]. The diffusion barriers \( E_m(i,q) \) of dominant defects were calculated by climbed nudged elastic band method (CI-NEB) [76,77] implemented within VASP.

III. RESULTS AND DISCUSSION

A. Formation of defects in LiF

The formation of defects depends on the properties of the specific material (e.g., band structure), the defects (e.g., defect structure and charge states), and the reservoir (e.g., \( \mu_{\text{Li}} \)). Figure 1 shows the formation energy \( (E_r) \) of several defects with low formation energies as a function of chemical potential \( \mu_{\text{Li}} \). The formation energy of each defect was obtained for the self-consistent (zero-charge) Fermi energy at each value of \( \mu_{\text{Li}} \).
In this \( \mu_{Li} \) range, the concentrations of \( V_{Li}^- \) and \( V_{F}^+ \) diverge significantly. In order to maintain the charge neutrality, holes are created. In this region, the Fermi level is very close to the top of the valence band (Fig. 2). As a result, holes can be generated by exciting electrons from the valence band to the defect levels \([6,52,53,55]\) induced by Li vacancies near the Fermi energy. In addition, the mass is conserved between LiF formation regions depending on the chemical potential \( \mu \).

FIG. 2. (Color online) Fermi energy of LiF as a function of the chemical potential \( \mu_{Li} \) in the reservoir.

In summary, there are two defect formation reactions in LiF depending on \( \mu_{Li} \) of the Li reservoir as follows.

1. LiF on high \( \mu_{Li} \) reservoirs (e.g., Li metal), the main reaction is
   \[
   \text{Li}_n\text{F}_n - \text{Li}_R^- - \text{FR} \xrightleftharpoons{\Delta G_i(\delta r)} \text{Li}_{n-1}\text{F}_{n-1} + V_{Li}^- + V_{F}^+, \tag{15}
   \]
   where \( \text{Li}_n\text{F}_n \) is the perfect LiF crystal, \( \text{Li}_R^-/\text{FR} \) refers to the Li/F reservoir, and this reaction has an increasing activation energy \( \Delta G_i(\delta r) = E_F(V_{Li}^-) + E_F(V_{F}^+) \) with increasing the separation \( (\delta r) \) of two vacancies.

2. LiF on low \( \mu_{Li} \) reservoirs (e.g., LiCoO\(_2\)), the main reaction is
   \[
   \text{Li}_n\text{F}_n - \text{Li}_R^- \xrightleftharpoons{\Delta G_p} \text{Li}_{n-1}\text{F}_{n-1} + V_{Li}^- + \oplus, \tag{16}
   \]
   where \( \oplus \) is a hole. This reaction has an activation energy \( \Delta G_p = E_F(V_{Li}^-) \).

According to reactions (15) and (16), we define three defect formation regions depending on \( \mu_{Li} \) of the reservoir (Fig. 3) and the dominant defect concentration as a function of \( \mu_{Li} \) of the reservoir is calculated for each region as follows.

**Intrinsic region.** In this region, the hole concentration is at least 7–8 orders of magnitude lower than that of Schottky pairs. As a result, the defect formation can be approximated by the reaction (15) and the defect concentration can be estimated by
   \[
   S(V_{Li}^-) = S(V_{F}^+) = N_c\exp(-\Delta G_i(\delta r)/k_B T), \tag{15}
   \]
   where, as discussed, \( \Delta G_i(\delta r) \) depends on the distance of the pair items \( V_{Li}^- \) and \( V_{F}^+ \). In Fig. 3, the left-triangle line (nearest-neighbor SP with the lowest \( \Delta G_i \)) and right-triangle line (dilute SP with the highest \( \Delta G_i \)) correspond to the two limits of the concentration of SP in this region, respectively. As a result, the majority ionic carriers in the intrinsic region are SPs \( (V_{Li}^- \text{ and } V_{F}^+ \text{ pairs}) \).

**p-type region.** The defect formation is dominated by the reaction (16), forming mainly \( V_{Li}^- \) and \( V_{F}^+ \) start to diverge and the dominant defect type changes from SP (intrinsic region) to \( V_{Li}^- \) \( (p\text{-type region}) \). The excess charge on \( V_{Li}^- \) which is not balanced by \( V_{F}^+ \) is balanced by holes. In order to calculate the defect concentration in this region, we use a charge balance concept by defining a portion \( p \) of \( V_{Li}^- \) whose charge is balanced by \( V_{F}^+ \). By this definition, \( 1 - p \) corresponds to the portion of \( V_{Li}^- \) in which the localized negative charge is balanced by holes. The starting point of this region is chosen from the point of \( \mu_{Li} \) that the concentration of holes is about 10 orders of magnitude less than that of SP. This type of \( V_{Li}^- \) is depicted as up-triangle line in the transitional region depicted in Fig. 3. Therefore, \( p \) can be determined by
   \[
   \frac{1 - p}{p} = \frac{n_\oplus}{N_{SP}}, \tag{17}
   \]

**B. Consideration of computational errors and comparison with experiments**

Density functional theory with generalized gradient approximation (DFT-GGA) is known to have its own deficiencies which may lead to errors in the density of states in the conduction band and the value of band gap \( (E_g = E_C - E_V) \) \([78]\). In our calculations, the influences of several possible errors were considered: (1) the value of \( N_C \), (2) the value of \( \varepsilon_F \), and (3) the underestimation of \( E_F(i,q) \) of defects with the defect induced electronic states occupied \( (\text{e.g., } V_{Li}^-/\text{Li}_0, V_{F}^+) \) \([79]\). To minimize the influence of these errors, we did the following corrections and considerations: (1) \( N_C \) was corrected by the ratio of the...
effective mass of electrons ($m^+_e$) [69] and holes ($m^+_h$) [80] in LiF with the relationship $N_c/N_i = (m^+_e/m^+_h)^{3/2}$ [1, 2], (2) we tested the sensitivity of $\varepsilon_F$ to the value of $E_g$ by using the experimental value $E_g^{\text{exp}}$ [58–60] and found that they were not sensitive to $E_g^{\text{DFT-GGA}}$ and $E_g^{\text{exp}}$ ($E_g^{\text{DFT-GGA}} < E_g^{\text{exp}}$) in LiF. It is because that $E_g^{\text{DFT-GGA}}$ is high enough to prevent free electrons in the conduction band [Eqs. (3) and (6a)] in LiF; and (3) $V_{\text{Li}}^-$ is formed by removing a Li$^+$ ion from a Li lattice site and the sixfold coordinated $F^-$ remain as $F^-$ ions. However, for $V_{\text{Li}}$, one of the nearest-neighbor $F^-$ ions becomes a neutral $F$ atom. Because the excess electron in the $V_{\text{Li}}^-$ system stays at the F-2p orbital (near valence band maximum), DFT-GGA can predict a reliable value of the formation energy of $V_{\text{Li}}^-$ [79].

In addition, for defects that can have their defect induced electronic states near the conduction band minimum (e.g., Li$_1$, $V_F$), their $S(i, q)$ are very low. We think that the errors that DFT-GGA can overestimate $S(i, q)$ would be insignificant. Therefore, we expect the influence of the errors in determining main defect types negligible.

Our results are consistent with experimental values [81–83]. The intrinsic defect formation energy [reaction listed in (15)] was extrapolated from ionic conduction measurement of divalent ion (e.g., Mg$^{2+}$) sensitive to $\gamma$ in (15) was extrapolated from ionic conduction measurement.

According to the definition of $\Delta G_{\text{exp}}$, our results predict the theoretical two limits for $\Delta G_{\text{exp}}$: 2.24 eV (nearest-neighbor SP) and 2.94 eV (dilute SP). The experimental value of $\Delta G_{\text{exp}}$ is $\approx 2.68$ eV [81–83] with an individual $V_{\text{Li}}^-$ formation energy $\Delta G_{V_{\text{Li}}^-} \approx 0.73$ eV [85].

C. Diffusion barriers of dominant defects

1. Diffusion of dilute vacancies in LiF

We studied the diffusion barriers of the main defects in LiF ($V_{\text{Li}}^-$ and $V_{\text{F}}^+$) through CI-NEB calculations [76, 77]. Since $V_{\text{Li}}^-\, \text{and } V_{\text{F}}^+$ sites maintain the same symmetry, we constructed two diffusion pathways for each: through face center (FC, along [110] direction) and through body center (BC, along [111] direction). For $V_{\text{Li}}^-$, after relaxation, the saddle point of the constructed BC path relaxed to a point between FC and BC (shown in Fig. 4 inset: path 2). The diffusion barrier for $V_{\text{Li}}^-$ is slightly smaller for path 2 ($\approx 0.57$ eV) than that for path 1 (FC path, $\approx 0.60$ eV), although path 2 has a larger travel distance than path 1. However, for $V_{\text{F}}^+$, two constructed pathways relaxed to the same saddle point (FC path) with a 0.69 eV diffusion barrier. The higher diffusion barrier for $V_{\text{F}}^+$ can be attributed to that $F^-$ has a larger ionic radii compared with Li$^+$.

2. Diffusion of nearest-neighbor Schottky pair

It is important to discuss the motion of neutral nearest-neighbor SP and its contribution to the ionic conductivity, since it has a higher concentration compared with dilute SP in the intrinsic region. We considered two mechanisms for nearest-neighbor SP to diffuse in the LiF: (1) nearest-neighbor SP diffuses together to its nearest available site and (2) nearest-neighbor SP separates to $V_{\text{Li}}^-$ and $V_{\text{F}}^+$ and then diffuse. In an ionic conductivity measurement [84], the first mechanism is not counted since the nearest-neighbor SP does not carry any net charge [Eq. (13)].

As a result, the second mechanism is considered in our ionic conductivity calculations. The disassociation energy barrier ($\Delta G_d$, shown in Fig. 5) is estimated based on two assumptions: (1) $V_{\text{Li}}^-$ is more mobile than $V_{\text{F}}^+$ (Sec. III C 1) and (2) nearest-neighbor SP dissociates when $V_{\text{Li}}^-$ diffuses to its next nearest neighbor (shown in inset of Fig. 5). This disassociation energy ($\approx 0.6$ eV) is added to estimate the contribution of nearest-neighbor SP to ionic conduction. The contribution of nearest-neighbor SP to the total ionic conductivity is about five orders of magnitude lower than that from dilute SP at room temperature. Although the second nearest-neighbor SP is not well separated (about 0.1 eV lower in energy than dilute SP), we would expect the contribution of nearest-neighbor SP to be very small.
D. Ionic conduction in LiF

The ionic conductivity is calculated according to the main defects in each region defined in Sec. III A.

**Intrinsic region:**

\[ \sigma = \sigma_{SPd} + \sigma_{SPn} \approx \frac{q^2 F^2}{RT} \left[ S_{SPd} + S_{SPn} \exp \left( \frac{-\Delta G_d}{k_B T} \right) \right] \left( D_{V_{Li}^+} + D_{V_{Li}^-} \right). \]  \tag{19}

where \( \Delta G_d \) is the dissociation energy calculated in Sec. III C 2; \( S_{SPd} \) and \( S_{SPn} \) are the concentration of dilute and nearest-neighbor SP. Since \( V_F^0 \) has \(-0.12\) eV higher in migration barrier compared with \( V_{Li}^- \), its contribution is insignificant to the total ionic conduction.

**Transitional region:**

\[ \sigma = \sigma_{V_{Li}^+} + \sigma_{SPd} + \sigma_{SPn} \approx \sigma_{V_{Li}^-} + \sigma_{SPd} \approx \frac{q^2 F^2}{RT} \left[ p S_{V_{Li}^+} (D_{V_{Li}^+} + D_{V_{Li}^-}) + (1 - p) S_{V_{Li}^-} D_{V_{Li}^-} \right]. \]  \tag{20}

where \( p \) is the portion of \( V_{Li}^- \) whose charge is balanced by the formation of \( V_{Li}^+ \) as defined in Sec. III A. In this region, we neglect the contribution from nearest-neighbor SP due to the following: (1) its small contribution compared with dilute SP; (2) in this region, the contribution from \( V_{Li}^- \) becomes dominant especially when approaching \( p \)-type region.

**\( p \)-type region:**

\[ \sigma = \sigma_{V_{Li}^+} = \frac{F^2 q^2}{RT} S_{V_{Li}^+} D_{V_{Li}^-}. \]  \tag{21}

The calculated results are shown in Fig. 6. The activation energy \( (E_f + E_m \approx 2.03 \text{ eV}) \) in the intrinsic region is comparable with experimental extrapolation \((1.99 \text{ eV}) \) to the intrinsic region at room temperature. The ionic conductivity is small in the intrinsic region (high \( \mu_{Li} \)) and is increased dramatically when \( \mu_{Li} \) is below \(-4.6 \text{ eV}\). This dramatic increase in ionic conductivity is due to the formation of \( V_{Li}^- \) which is preferred at low \( \mu_{Li} \), and it is no longer constrained by the formation of \( V_F^0 \) to balance the charge (Fig. 3).

![Image](image.png)

**FIG. 6.** Ionic conductivity of LiF as a function of the chemical potential of Li reservoir. Inset: schematic drawing of LiF contacting a Li reservoir (e.g., an electrode for application of LIBs).

E. LiF as an engineered SEI for LIBs

Considering a solid electrolyte (an engineered artificial SEI) coated on electrodes for LIBs, the Li reservoir (inset in Fig. 6) can be viewed as an electrode on which the LiF is coated. For different electrodes (e.g., \( \mu_{Li-metal} \sim -2.02 \text{ eV}; \mu_{LiCoO_2} = -6.2 \text{ eV} \) or electrodes with different state of charge (e.g., LiC\(_{12}, \) LiC\(_5\)), the values of \( \mu_{Li} \) are different. In electrochemistry, the electrochemical potential of Li\(^+\) in a spatial point is defined as \([86]\)

\[ \tilde{\mu}_{Li^+} = \mu_{Li^+} + z_i F \phi, \]  \tag{22}

where \( \tilde{\mu}_{Li^+} \) is the electrochemical potential, \( \mu_{Li^+} \) is the chemical potential of Li\(^+\), \( z_i \) (\( z_i = 1 \) for Li\(^+\)) is the associated charge, and \( \phi \) is the electrical potential in that spatial point. At thermodynamic equilibrium, the electrochemical potential is the same everywhere in a battery (i.e., \( \mu_{Li}^{\text{cathode}} = \mu_{Li}^{\text{anode}} \)). Under this condition, we can estimate the cell voltage by

\[ V = \phi^{\text{cathode}} - \phi^{\text{anode}} = -\frac{\mu_{Li}^{\text{cathode}} - \mu_{Li}^{\text{anode}}}{F}. \]  \tag{23}

By assuming \( \mu_{Li} \approx \mu_{Li^+} + \mu_{Co} \) in the electrode and the same wire (e.g., copper) used to connect the cathode and anode \( (\mu_{Co} = \mu_{anode}) \), the voltage of the cell can be estimated from the differences of \( \mu_{Li} \) in electrodes. This is the well-known Nernst equation in electrochemistry \([7]\). In LIBs, \( \mu_{Li} \) in Li metal is typically defined as a reference (zero volt). Therefore, we can relate \( \mu_{Li} \) in the reservoir to the open-circuit voltage of the electrodes (a half cell) by referencing to \( \mu_{Li} \) in Li metal

\[ V = -\left( \mu_{Li} - \mu_{Li-metal} \right)/e. \]  \tag{24}

The ionic conductivity \( \sigma \) in LiF highly depends on the electrode it contacts with. For example, if LiF is coated on a negative electrode surface (e.g., graphite, silicon), \( \sigma \) is very small\((\approx 10^{-30} \text{ S cm}^{-1})\). Compared with \( \sigma \) in other SEI species (e.g., Li\(_2\)CO\(_3\)), \( \sigma \) in LiF is 18 to 20 orders of magnitude lower. However, if it is coated on a positive electrode (e.g., LiCoO\(_2\)), \( \sigma \) is controlled by free \( V_{Li}^- \) diffusion and it is comparable with other SEI species (e.g., Li\(_2\)CO\(_3\)). This result is significant since it demonstrates that the ionic conductivity of LiF is strongly voltage dependent. Therefore, higher doping of divalent cation (e.g., Mg\(^{2+}\)) is suggested to improve Li ion conductivity of LiF coating on negative electrodes by increasing the concentration of diffusion carrier \( V_{Li}^- \).

The ionic transport contributes to the electrical conduction in the lithium crystal (e.g., LiF) \([1,2]\). It can be expected that LiF is more electrical insulating on the negative electrode than other species (e.g., Li\(_2\)CO\(_3\)) due to its low ionic conductivity. It was believed that the electron leakage from the electrode is an important step in the ethylene carbonate decompositon leading to SEI formation \([22–24]\). Various groups have reported fluoroethylene carbonate (FEC) as an electrolyte additive that can improve the performance of Si electrode with increased LiF formation in the SEI layer \([42–47]\). Our results provide a reason for this observation that LiF on the negative electrode surface can better passivate the electrode surface and prevent electron leakage. As a result,
it can cause less capacity loss and longer cycling life of the electrode.

IV. CONCLUSIONS

We developed a method to study the defect physics in a material in equilibrium with an external phase. This method establishes a correlation between the open-circuit voltage and Li chemical potential in the electrodes. We applied this approach to study defect reactions in LiF in contact with different electrode materials which serve as Li reservoirs. We demonstrated that the defect formation in a solid electrolyte can be affected by the open-circuit voltage of the electrode, which is a measurable and controllable parameter. Three regions (intrinsic, transitional, and p-type) were defined to describe the main defect reactions with different electrodes. We found that the main defect type in the intrinsic region (high $\mu_{Li}$ reservoirs) was Schottky pair and in the p-type region (low $\mu_{Li}$ reservoirs) was Li-ion vacancy. The diffusion barrier of main defects in each region was estimated from CI-NEB calculation and mapped to ionic conduction based on the Nernst-Einstein formula. The ionic conductivity is very low ($10^{-31}$ S cm$^{-1}$) in the intrinsic region and increases (to $10^{-12}$ S cm$^{-1}$ when $\mu_{Li} \approx -6.5$ eV) with increasing the voltage of the nearby electrode. Thus, the ionic conduction in a solid electrolyte is very sensitive to the external potential of the electrode on which the electrolyte material is coated. This work extends the well known relationship between defect concentration and chemical potential for gas phase reactions to electrochemical reactions.

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