Hybrid PV-Wind, Micro-Grid Development Using Quasi-Z-Source Inverter Modeling and Control—Experimental Investigation

Neeraj Priyadarshi  
*Millia Institute of Technology, India*

Sanjeevikumar Padmanaban  
*Aalborg University, Denmark*

Dan M. Ionel  
*University of Kentucky, dan.ionel@uky.edu*

Lucian Mihet-Popa  
*Østfold University College, Norway*

Farooque Azam  
*Millia Institute of Technology, India*

Right click to open a feedback form in a new tab to let us know how this document benefits you.

Follow this and additional works at: [https://uknowledge.uky.edu/peik_facpub](https://uknowledge.uky.edu/peik_facpub)  
Part of the [Power and Energy Commons](https://uknowledge.uky.edu/peik_facpub)

Repository Citation

[https://uknowledge.uky.edu/peik_facpub/1](https://uknowledge.uky.edu/peik_facpub/1)

This Article is brought to you for free and open access by the Power and Energy Institute of Kentucky at UKnowledge. It has been accepted for inclusion in Power and Energy Institute of Kentucky Faculty Publications by an authorized administrator of UKnowledge. For more information, please contact UKnowledge@lsv.uky.edu.
Abstract: This research work deals with the modeling and control of a hybrid photovoltaic (PV)-Wind micro-grid using Quasi Z-source inverter (QZsi). This inverter has major benefits as it provides better buck/boost characteristics, can regulate the phase angle output, has less harmonic contents, does not require the filter and has high power performance characteristics over the conventional inverter. A single ended primary inductance converter (SEPIC) module used as DC-DC switched power apparatus is employed for maximum power point tracking (MPPT) functions which provide high voltage gain throughout the process. Moreover, a modified power ratio variable step (MPRVS) based perturb & observe (P&O) method has been proposed, as part of the PV MPPT action, which forces the operating point close to the maximum power point (MPP). The proposed controller effectively correlates with the hybrid PV, Wind and battery system and provides integration of distributed generation (DG) with loads under varying operating conditions. The proposed standalone micro grid system is applicable specifically in rural places. The dSPACE real-time hardware platform has been employed to test the proposed micro grid system under varying wind speed, solar irradiation, load cutting and removing conditions etc. The experimental results based on a real-time digital platform, under dynamic conditions, justify the performance of a hybrid PV-Wind micro-grid with Quasi Z-Source inverter topology.

Keywords: PV; MPRVS; Quasi Z-source inverter; MPP; SEPIC converter

1. Introduction

Micro-grid comprises the combination of interconnected loads and distributed energy resources (DER), including energy storage devices and several active loads/prosumers which work as a controlled unit to deliver the electric demand for miniature location. It supplies power generation with tremendous reliability as well as an affirmation to varying loads [1–3]. Fossil fuels and nuclear sources are treated as the traditional energy sources, which provide electricity and are not located closer to the load point. As the conventional energy sources are not environmentally friendly and due to the long-distance transmission, there are considerable power losses that can occur. Therefore, nowadays, renewable energy sources have been given more attention by the researchers and industry to generating alternative power [4–12]. Distributed generating (DG) source such as solar, wind, fuel...
cell, hydro, tidal, etc. are considered as the main renewable technology, which is highly flexible, expandable and has environmentally friendly behavior. The maximum power point tracking (MPPT) is the important constituent needed to achieve the maximum power point (MPP) as an operating point which enables the utmost power extraction for renewable sources [13,14]. Several MPPT techniques, including Perturb & Observe (P&O), Incremental Conductance (INC), Fuzzy logic control (FLC), Artificial Neural Network (ANN), Particle swarm optimization (PSO), Ant Colony Optimization (ACO), Artificial Bee Colony (ABC), Firefly Algorithm (FA) etc. reviewed in the literature were unable to detect global peak point with partial shade situations [15–27]. In this work, Modified Power Ratio Variable Step (MPRVS) based on the P&O technique is proposed without the proportional-integral (PI) controller utilization, which reduces power oscillation near to MPP in comparison to a conventional P&O algorithm and also provides the prevention to battery charging from voltage fluctuation.

To avoid multi reversal generation occurrence in a micro-grid system, in the current research, a Quasi Z-Source inverter is employed [28–33]. The DC-DC converter is a vital interface to achieve a peak power generation from PV modules. In this work, a high-quality tracking behavior is achieved by employing single ended primary inductance converter (SEPIC), which provides high voltage gain with better buck/boost performance compared to other dc-dc switched power converters [34]. In this paper, an additional dc-dc converter (SEPIC converter) is used because it comprises buck/boost capabilities. Moreover, QZsi combines a boost converter and an inverter. The MPRVS based P&O MPPT is controlled through the SEPIC converter which provides MPP achievement and works effectively under varying sun insolation and wind velocity. Moreover, the SEPIC converter works as an impedance adapter between the PV panel and Z-source inverter. Jain et al. [35] have implemented QZsi based grid PV system using a predictive controller in which the active and reactive power have been regulated. However, this work is discussed only for the PV system which utilized the traditional INC MPPT with a classical PI controller as a dc bus regulator. Liu et al. [36] have discussed QZsi based multilevel inverter for grid PV power system, which provides precise MPPT and dc-link voltage regulation at the unity power coefficient. However, during practical justification, voltage/current sensors and bulk resistor models are required, which has a high cost. Nevertheless, this work only explains the performance of QZsi based multilevel inverter for only the PV systems rather than the hybrid system. Amini et al. [37] have discussed the cloud computing applications in micro grid clusters. A real time digital simulator is employed for the physical interpretation of power routing which can be utilized for electrical grid utility with the communication system. However, the application of the proposed scheme with hybrid PV-Wind micro grid systems is missing in this research work. Ali et al. [38] have conferred game theory structure for improvement of smart grid efficiency in which the Femtocell communication system is employed. However, the main disadvantage of this proposed communication system is interference in cross layer. Furthermore, the proposed game theory application with hybrid PV-Wind micro grid system has not been discussed in this research work. Vignesyn et al. [39] have discussed the hybrid micro grid for standalone/Grid mode operation with Z-source inverter. This paper discusses the behavior of micro grid under varying loading conditions, solar insolation and wind speed using simulation environment (MATLAB) only. The real time implementation is missing in this research work. In this research work, to reduce multiple reverse conversions and for improving the efficiency of the micro grid, hybrid PV-Wind with Quasi Z-source inverter has been implemented. Furthermore, SEPIC converter acts as a dc link interface with MPPT functioning. This research work is organized under 3 main sections. Section 1 discusses the micro-grid system with an extensive literature review of MPPT techniques, dc-dc converters with benefits of Z-source inverter. Section 2 presents the complete structure of the hybrid PV-Wind micro-grid system. It explains the PV generator modeling, wind turbine model, MPRVS based MPPT algorithm, design specifications of SEPIC converter, battery model as well as the modes of operations of the Quasi Z-source inverter. Section 3 presents the experimental results which validate the performance of the proposed hybrid PV-wind micro-grid system. The novelty of this research paper is MPRVS based advanced MPPT algorithm have neither
been dis-coursed nor been utilized before for the hybrid PV-wind micro-grid with Quasi Z-source inverter experimentally.

2. Hybrid PV-Wind Micro Grid Structure

The proposed structure of the PV-Wind micro grid system is shown in Figure 1. The micro grid system contains a PV generator, a Wind Turbine, a battery system and the power electronic converter topologies. To analyze the proposed system, the equivalent circuit with two diode models for the PV generator has been used because of its better power extraction capability when compared with the single diode model. The rotor of the wind turbine is mechanically tied to a generator to produce electrical power. A wind turbine is a complex system, but a reasonably simple representation is possible by modeling the aerodynamic torque or power based on turbine characteristics (non-dimensional curves of the power coefficient). A battery solution is also necessary to balance the stochastic fluctuations of photovoltaic (PV) power and wind power injected to the grid/load. In this section, a short description about how these main components of the proposed micro grid system have been modeled are presented.

![Figure 1](image1.png)

**Figure 1.** A block diagram with the structure of Hybrid PV-Wind micro grid system.

2.1. PVG Mathematical Model

Figure 2 illustrates the basic PV cell schematic diagram, which is responsible for the transformation of the solar energy into electric power using photoelectric effect which comprises numerous cells. In this paper, the two-diode model is considered to deliver better accuracy compared to the single diode model.

![Figure 2](image2.png)

**Figure 2.** Equivalent circuit model of a PV cell with double diodes and a series and parallel resistance.
The PV cell output current is expressed mathematically as:

\[ I_N = I_{\text{Photon}} - I_{\text{Diode1}} - I_{\text{Diode2}} - \left( \frac{V_N + I_N R_{\text{SE}}}{R_{\text{Parallel}}} \right) \]  

(1)

Also, Photon current is evaluated mathematically as:

\[ I_{\text{Photon}} = [I_{\text{Photon,STC}} + K_S(T_C - T_{\text{STC}})] \times \frac{G}{G_{\text{STC}}} \]  

(2)

Diode saturation current can be expressed as:

\[ I_{\text{Diode1}} = I_{\text{Diode2}} = \frac{I_{\text{Short,STC}} + K_S(T_C - T_{\text{STC}})}{\exp\left(\frac{(V_{\text{pec,STC}} + K_V(T_C - T_{\text{STC}}))}{V_{\text{Thermal}}}\right) - 1} \]  

(3)

### 2.2. Wind Turbine Modeling

A wind turbine is essentially a machine that converts the kinetic energy first into mechanical energy at the turbine shaft, and then into electrical energy. The wind turbine power generation depends mainly on wind velocity in which the rotors are mechanically linked to a generator. A simple model can be achieved by using the power coefficient (CPR) as a function of tip speed ratio and the blade pitch angle. CPR (Performance / power coefficient) Vs tip speed (\( \lambda_{T,S} \)) curve is plotted for different \( \beta_{P,B} \) (Pitch blade angle) in Figure 3.

![Figure 3. CPR (Performance coefficient) Vs tip speed (\( \lambda_{T,S} \)) curve plotted for different \( \beta_{P,B} \) (Pitch blade angle).](image)

Generated mechanical power output from the wind turbine can be written using Equation (4) which is depending on wind velocity (\( V_{\text{Wind}} \)), \( R_T \) (Turbine radius) and \( C_{PR} \) (Performance coefficient) as:

\[ P_{\text{Mechanical}} = \frac{1}{2} C_{PR} \pi R_T^2 \rho_{\text{air}} d V_{\text{Wind}}^3 \]  

(4)

Also, the ratio of tip speed (\( \lambda_{T,S} \)) can be described mathematically which is correlated with an angular velocity of the blade (\( \omega_{A,V} \)), \( V_{\text{Wind}} \) and \( R_T \) as:

\[ \lambda_{T,S} = \frac{\omega_{A,V} \times R_T}{V_{\text{Wind}}} \]  

(5)
And coefficient of performance is expressed with $\lambda_{TS}$ and $\beta_{P,B}$ (Pitch blade angle) as:

$$
C_{PR}(\lambda_{TS}, \beta_{P,B}) = 0.72 \left[ \frac{150}{\lambda_j} - 2 \times 10^{-3} \beta_{P,B} - 131 \times 10^{-1} \right] e^{\frac{-185 \times 10^{-1}}{\gamma}}
$$

(6)

where,

$$
\frac{1}{\lambda_j} = \frac{1}{(\lambda_{TS} + 8 \times 10^{-2} \beta_{P,B})} - 35 \times 10^{-3} \left( \frac{1}{1 + \beta_{P,B}^2} \right)
$$

(7)

$$
\lambda_{TS} = \frac{\omega_G \times R_T}{V_{Wind} \times \eta_{gear}}
$$

(8)

$$
\eta_{gear} = \frac{\omega_{GM} \times R_T}{\lambda_{TS} V_{Wind}}
$$

(9)

2.3. Electric Equivalent Circuit of the Battery Model

A battery is a vital component for a hybrid system which provides the solution under fluctuating action of renewable energy sources. In this work, the electric circuit-based battery model is employed, which provides better dynamics for a state of charge operation mode. It comprises a voltage source (ideal) with a series of internal resistance which evaluates the battery behavior as depicted in Figure 4.

![Figure 4. Electric equivalent circuit-based battery model.](image)

Final voltage controlled is obtained mathematically as:

$$
V = E_B - \frac{V_{PO} \times Q_{Bat}}{Q_{Bat} - \int I_{Battery} dt} + A_{exp} \cdot e \left( B_{exp} \int I_{Battery} dt \right)
$$

(10)

3. Power Electronic Converters used to Control the Proposed Micro Grid System. Description and Mathematical Modelling

The power converters have been developed to manage the maximum energy harvesting and power processing for the hybrid solution with Photovoltaic (PV) and wind power generators. The topologies involved in this study contains two topologies of power electronic converters: a SEPIC converter and a Quasi Z-Source Inverter (QZsi). The MPPT method for QZsi is introduced based on the P&O method to minimize the voltage stress on the inverter. Moreover, it prevents overlapping between Shoot-Through (ST) duty ratio and modulation index using DC-Link voltage controller. The output current is regulated using the stationary frame current controller, achieving lower Total Harmonic Distortion (THD) as much as possible. The SEPIC based soft switching for MPPT action is controlled through an advanced MPRVS based P&O MPPT. A quasi Z-source inverter with the common grounding characteristics is employed to get high voltage gain. Employed inverter operates in two modes of operation as the shoot through and the non-shoot through the states.
3.1. SEPIC Converter Model

Single ended primary inductor converter (SEPIC) is considered as an impedance adapter between the PV module and the Z-source inverter as it provides high gain throughout the operation, better voltage performance and high voltage rating for lower/higher power requirements. When boost converter combines with the additional inductor and the capacitor, a SEPIC converter is developed. In contrast with the buck boost converter, the polarity of SEPIC is kept positively as it is depicted in Figure 5. Table 1 portrays the employed SEPIC converter parameters during an implementation.

\[ V_{output} = V_{supply} \times \frac{D_{duty}}{1 - D_{duty}} \]

\[ L_A = \frac{V_{supply} \times D_{duty}}{\Delta I_A \times f_{switching}} \]

\[ L_B = \frac{V_{supply} \times D_{duty}}{\Delta I_B \times f_{switching}} \]

\[ C_A = \frac{V_{output} \times D_{duty}}{R_{Load} \times \Delta V_o \times f_{switching}} \]

\[ C_B = \frac{V_{output} \times D_{duty}}{R_{Load} \times \Delta V_o \times f_{switching}} \]

![Figure 5. SEPIC converter equivalent circuit.](image)

<table>
<thead>
<tr>
<th>Sl. No.</th>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>Inductors ((L_A = L_B))</td>
<td>0.42 mH</td>
</tr>
<tr>
<td>2.</td>
<td>Capacitors ((C_A = C_B))</td>
<td>(3.5 \times 10^{-3}) μF</td>
</tr>
<tr>
<td>3.</td>
<td>Current ripple ((\Delta I_{i_A} = \Delta I_{i_B}))</td>
<td>0.5 A</td>
</tr>
<tr>
<td>4.</td>
<td>Voltage ripple ((\Delta V_o))</td>
<td>(1 \times 10^{-3}) V</td>
</tr>
<tr>
<td>5.</td>
<td>Switching frequency ((f_{switching}))</td>
<td>20 Hz</td>
</tr>
</tbody>
</table>

3.2. Modified Power Ratio Variable Step Based P&O MPPT

Figure 6 demonstrates the working model of MPRVS based P&O technique for optimal PV power extraction from solar modules. The generation of gating pulses to the SEPIC converter is possible without the action of the PI controller, which makes the reduction of power oscillation nearer to MPP and forces operating point close to the MPP. It also prevents the battery charging system from over voltage. The instantaneous power obtained through PVG \([P_{PV}(N)]\) at SEPIC output terminal is calculated as:

\[ P_{PV}(N) = V_0(N) \times I_{PV}(N) \]

Also, the previous instantaneous power is mathematically described as:

\[ P_{PV}(N - 1) = V_{PV}(N - 1) \times I_{PV}(N - 1) \]
Figure 6. Working model of MPRVS based P&O technique.

3.3. Quasi Z-Source Inverter Mathematical Modeling

Figure 7 presents the equivalent power circuit of Quasi Z-source inverter which comprises of L_A, L_B, C_A, C_B components with impedance circuit. The considered Z-Source Quasi inverter has no filter requirement, better buck/boost characteristics, able to regulate the phase angle output, less size, continuous conducting mode working, less harmonic content, high efficiency and with better power performance over the conventional inverter as major advantages. The Quasi Z-source inverter operates in two modes of operation. In the non-shoot mode, the equivalent circuit has 6 active states with 2 zero states. The T_S is the total switched inverter with T_A and T_B as the shoot through the state and the non-shoot through state, respectively. The duty ratio \( D_{duty} \) of SEPIC converter is mathematically written as:

\[
D_{duty} = \frac{T_A}{T_S} \tag{22}
\]

Mode I: The equivalent model of Quasi Z-source inverter is depicted in Figure 8 and mathematical equations governing non-shoot through the state is expressed as:

\[
\begin{align*}
V_{L_A} &= V_{IN} - V_{C_A} \\
V_{L_B} &= -V_{C_B} \\
V_{DIODE} &= 0
\end{align*} \tag{23}
\]

Mode II: Figure 9 illustrates the equivalent model of Quasi Z-source inverter in shoot through the state mode with the mathematical expression as:

\[
\begin{align*}
V_{L_A} &= V_{IN} + V_{C_A} \\
V_{L_B} &= V_{C_B}
\end{align*} \tag{24}
\]
\[ V_{\text{DIODE}} = V_{CA} + V_{CB} \]

![Figure 7. Equivalent power circuit of Quasi Z-source inverter.](image)

![Figure 8. The equivalent model of Quasi Z-source inverter governing non-shoot through the state.](image)

![Figure 9. Equivalent model of Quasi Z-source inverter in shoot through the state.](image)

Under the steady condition, the average inductor voltage becomes zero.

\[ V_{LA} = \left[ \frac{(V_{IN} + V_{CB})T_A + (V_{IN} - V_{CA})T_B}{T_S} \right] = 0 \]  \hspace{1cm} (25)

\[ V_{LB} = \left[ \frac{V_{CA}T_A + (-V_{CB})T_B}{T_S} \right] = 0 \]  \hspace{1cm} (26)
On solving the above equations, capacitor voltage \( V_{CA} \) and \( V_{CB} \) is calculated mathematically as:

\[
V_{CA} = \left( \frac{T_B}{T_B - T_A} \right) \times V_{IN} \tag{27}
\]

\[
V_{CB} = \left( \frac{T_A}{T_B - T_A} \right) \times V_{IN} \tag{28}
\]

Maximum voltage across DC-link = \( V_{CA} + V_{CB} \) \tag{29}

Putting Equations (26) and (27) in (28) we get

\[
\text{Maximum DC-link voltage} = \left| \frac{1}{1 - 2 \frac{T_A}{T_S}} \right| V_{IN} = K \times V_{IN} \tag{30}
\]

4. Experimental Setup Description and Results

4.1. Description of the Experimental Setup

The considered hybrid PV-Wind micro grid is tested using MPRVS based P&O MPPT with employed Z-source inverter. Figure 10 depicts the developed practical structure of the proposed hybrid micro grid based on a real-time platform, dSPACE. The SEPIC converter is controlled through the MPRVS based P&O based MPPT, in which LV-25P and LA-25P, current and voltage sensors are employed for measuring the PV panel parameters, \( V_{PV} \) and \( I_{PV} \) respectively. The power factor coefficient and THD are evaluated using the power quality analyzer (FLUKE 43B), considering the main components of the converter: IGBT (IRG4PH50U), diode (Freewheel RHG30120), driver circuit (HCPL 3120) etc. permanent magnet synchronous generator (PMSG) based wind emulator system is employed as the wind turbine generator and is mechanically coupled with the DC-motor. The switched mode power converter makes the wind turbine to have varying wind speed which produces the required mechanical torque by controlling wind turbine characteristics.

![Figure 10](image-url)
4.2. Experimental Results and Scenarious Development

The accuracy of the proposed MPRVS based P&O MPPT has been tested with changing wind operating condition depicted in Figure 11a. The employed controller works in MPP area and provides optimal tracking of wind power under the sudden changes of wind velocity shown in Figure 11b. The corresponding duty ratio of SEPIC converter is shown in Figure 11c. Furthermore, the capability of proposed MPPT tracker is examined under the first scenarios with step varying solar irradiation. Figure 12 demonstrates that the PV array has obtained parameters under the step-changes in solar irradiation and the propped system has proved high accuracy and effective PV tracking in MPP region. The obtained experimental results in Figure 13a illustrate that the performance of the proposed hybrid micro grid under the second scenarios by varying wind velocity and constant solar irradiation. Also, Figure 13b demonstrates the behavior responses of the hybrid micro grid under varying solar irradiance and constant wind velocity with MPRVS based P&O MPPT employed. The performance of the hybrid micro grid is also tested under the third proposed scenarios in the absence of wind velocity and during this operation: the load is connected/disconnected to the utility grid, which is shown in Figure 14a under the load cutting condition, and in Figure 14b, under the load removing conditions. The performance of the wind generator is evaluated under disconnecting/reconnecting operating conditions to the micro grid, which are depicted in Figures 15 and 16 and reveal that the accurate performance of the proposed hybrid micro grid in varying operating situations (disconnecting operating conditions to the micro grid and reconnecting operating conditions to the micro grid), respectively.

![Figure 11. Experimental results (a) during a step-changed in wind speed; (b) wind power; and (c) Duty cycle of Cuk converter.](image)
Figure 12. PV system responses under step-changes in solar irradiation.

Figure 13. (a) Capability of the proposed hybrid micro grid under varying wind velocity and constant solar irradiation; (b) Behavior responses of the hybrid micro grid under varying solar irradiance and constant wind velocity.

Figure 14. The performance of the hybrid micro grid (a) load cutting condition; (b) Load removing condition.
The two-diode model-based PV Generator provides high power extraction when compared to experimental results under dynamic conditions, such as step-changed in wind speed or solar irradiation. Conclusively, the Quasi Z-source inverter has been evaluated experimentally as a superior topology having better buck/boost characteristics with fast dc-link voltage regulation under different conditions.

5. Conclusions

The proposed hybrid PV-Wind micro-grid system using Quasi Z-source inverter is established practically and tested with the Real-time digital simulator dSPACE (DS 1104) platform. The point wise findings that have been included in this section are as follows:

(i) The MPRVS based P&O MPPT performance with SEPIC converter has been validated effectively, which delivers MPP achievement with low power oscillation for the PV system.

(ii) The performance of the Quasi Z-source inverter has been evaluated experimentally as having better buck/boost characteristics with fast dc-link voltage regulation under different operating conditions.

(iii) The proposed QZsi topology for a hybrid PV-Wind Turbine application in a micro grid enhanced reliability, good output power quality and efficiency improvements.

(iv) Experimental results under dynamic conditions, such as step-changed in wind speed or solar irradiation, reveal that optimal power has been tracked through the PV-Wind renewable sources and proved the validity of the proposed solution.

(v) The two-diode model-based PV Generator provides high power extraction when compared to the single diode model.
As a future work, the paper can be extended by using the multilevel inverter with the application of advanced intelligent MPPT algorithms viz. Jaya DE, hybrid ANFIS-ABC methods.

**Author Contributions:** All authors contributed equally and formulated the research work to present in current version as full research article.

**Funding:** No funding addressed to this research activities.

**Conflicts of Interest:** The authors declare no conflict of interest.

**Nomenclature**

- $R_{SE}$: Resistance in series
- $R_{Parallel}$: Resistance in parallel
- $T_{STC}$: Temperature at STC (Standard Test Condition)
- $G_{STC}$: Solar irradiance at STC
- $K_S$: Coefficient of short circuit current
- $I_{Photon\_STC}$: Photo current at STC
- $T_C$: Ambient temperature
- $G$: Solar irradiation
- $I_{Short\_STC}$: Short circuit current at STC
- $V_{open\_STC}$: Open circuit current at STC
- $V_{Thermal}$: Diode thermal voltage
- $K_{VL}$: Voltage temperature coefficient
- $\rho_{a,d}$: Speed of generator
- $\omega_{GM}$: Peak allowed generator speed
- $\eta_{gear}$: Gear ratio
- $E_B$: Battery fixed voltage
- $V_{PO}$: Polarized voltage
- $Q_{Bat}$: Capacity of battery
- $I_{Battery}$: Battery current
- $A_{exp}$: Amplitude of exponential zone
- $B_{exp}$: Inverse time constant exponential zone
- $\Delta I_L = I_{Ls}$: Current ripple
- $\Delta V_0$: Ripple voltage
- $f_{switching}$: Switched frequency
- $V_0(N) & I_{PV}(N)$: Sensed voltage and current
- $\Delta D$: Step perturbation of duty ratio
- $dT$: Fixed step size
- $K$: Variable power ratio
- PI: Proportional Integral

**References**


